

Name:

Exam Style Questions

Trigonometry



Corbettmaths

Equipment needed: Calculator, pen

Guidance

1. Read each question carefully before you begin answering it.
2. Check your answers seem right.
3. Always show your workings

Video Tutorial

www.corbettmaths.com/contents

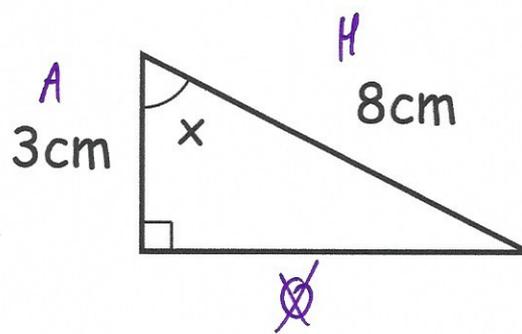
Videos 329, 330, 331



Answers and Video Solutions



1. Shown below is a right-angled triangle.



C^AH

Use trigonometry to work out the size of angle x.

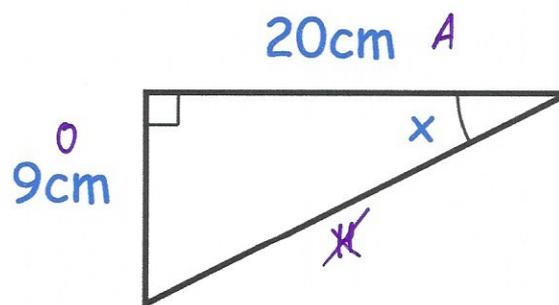
$$\cos x = \frac{3}{8}$$

$$x = \cos^{-1}\left(\frac{3}{8}\right)$$

$$\underline{\underline{67.98^\circ}}$$

(3)

- 2.



T^OA

Work out the size of angle x

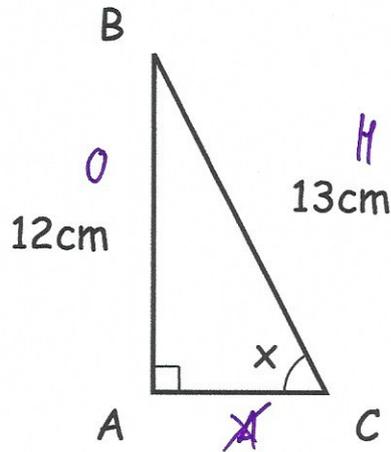
$$\tan x = \frac{9}{20}$$

$$x = \tan^{-1}\left(\frac{9}{20}\right)$$

$$\underline{\underline{24.23^\circ}}$$

(3)

3. ABC is a right-angled triangle



5° H

Work out the size of the angle marked x.

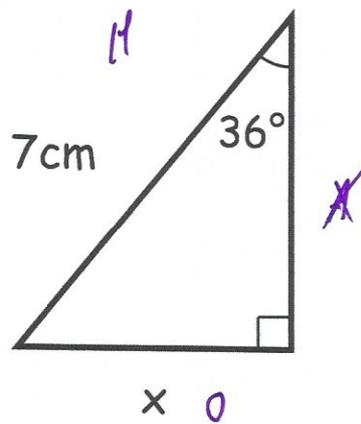
$$\sin x = \frac{12}{13}$$

$$x = \sin^{-1}\left(\frac{12}{13}\right)$$

67.38°

(3)

4. Below is a right-angled triangle.



5° H

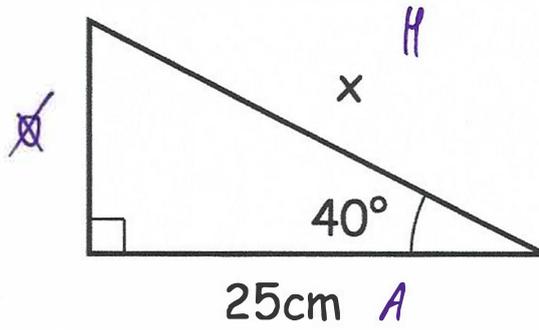
Use trigonometry to work out the length x.

$$x = \sin(36) \times 7$$

4.11 cm

(3)

5.



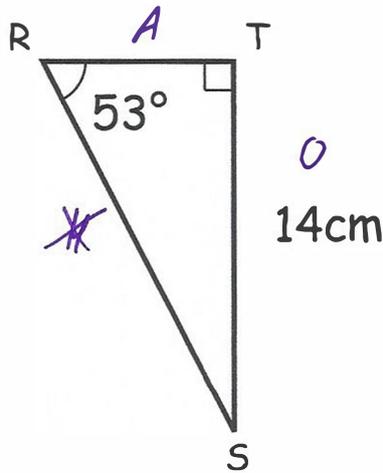
$C^A H$

Work out the length x .

$$x = \frac{25}{\cos 40}$$

32.64
.....cm
(3)

6.



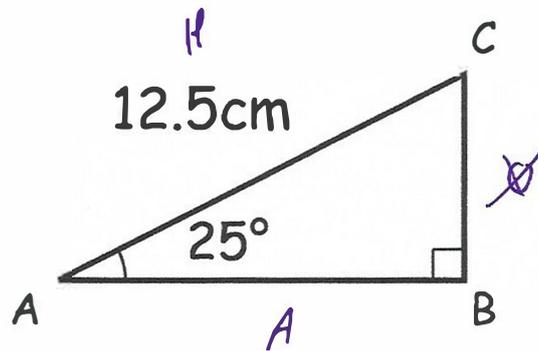
$T^O A$

Work out the length of RT.

$$RT = \frac{14}{\tan 53}$$

10.55
.....cm
(3)

7. Triangle ABC has a right angle.
 Angle BAC is 25°
 AC = 12.5cm



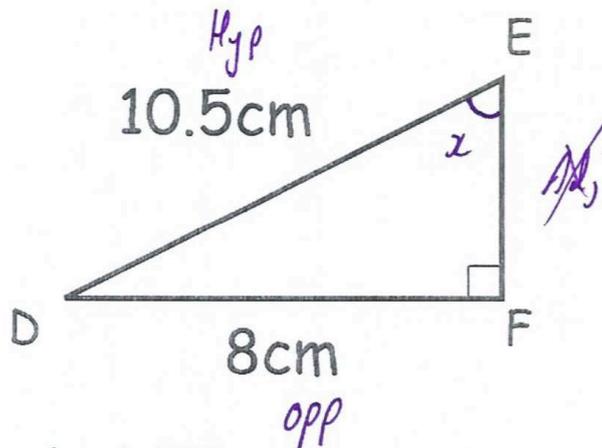
C A H

Calculate the length of AB

$$AB = (\cos(25)) \times 12.5$$

11.33
cm
 (3)

8. DEF is a right-angled triangle.



S O H

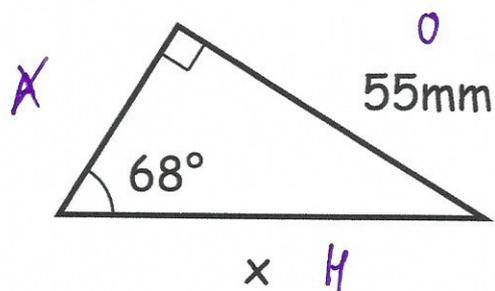
Calculate the size of angle DEF.

$$\sin x = \frac{8}{10.5}$$

$$x = \sin^{-1}\left(\frac{8}{10.5}\right)$$

49.63

 (3)



$5^\circ H$

Work out the length of side x .
Include suitable units.

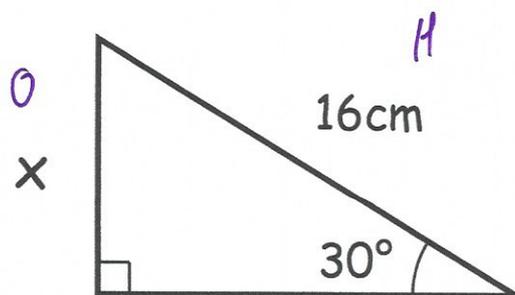
$$x = \frac{55}{\sin 68}$$

$$x = 59.32$$

59.32mm

(3)

10. Shown is a right-angled triangle



$$\sin 30^\circ = 0.5$$

Work out the value of x

$$x = \sin(30) \times 16$$

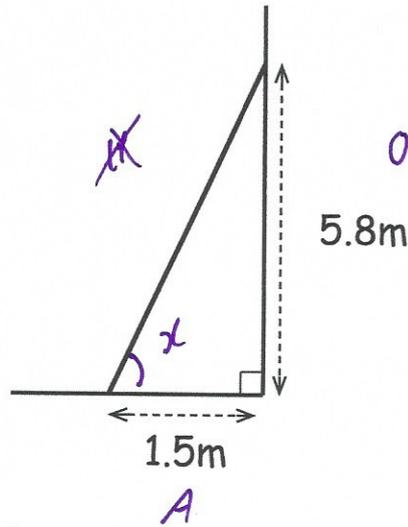
$$x = 0.5 \times 16$$

$$= 8\text{cm}$$

8cm

(3)

11. A ladder is placed against a vertical wall.
To be safe, it must be inclined at between 70° and 80° to the ground.



(a) Is the ladder safe?

$$\tan x = \frac{5.8}{1.5}$$

$$x = \tan^{-1}\left(\frac{5.8}{1.5}\right)$$

$$x = 75.5^\circ$$

Yes

(3)

(b) Calculate the length of the ladder.

Pythagoras:

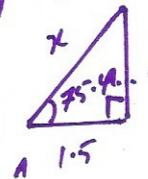
$$L^2 = 1.5^2 + 5.8^2$$

$$L^2 = 35.89$$

$$L = \sqrt{35.89}$$

$$L = 5.99$$

or Trigonometry



$$x = \frac{1.5}{\cos 75.4998\dots}$$

$$x = 5.99$$

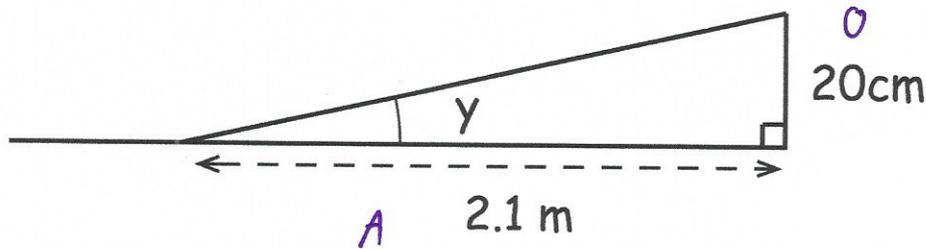
5.99

m
(3)

12. A ramp is built to help people enter a building.
 The start of the ramp is 2.1 metres from the base of the building.
 The ramp has a height of 20 centimetres.



T O A



Calculate the size of angle y .

$$\tan y = \frac{20}{210}$$

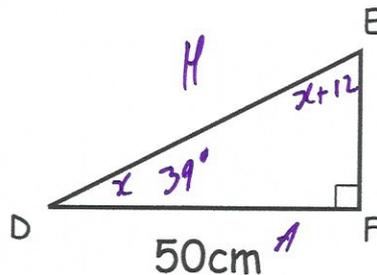
$$y = \tan^{-1}\left(\frac{20}{210}\right)$$

$$= 5.44$$

5.44

(3)

13. Shown below is right-angled triangle DEF.



$$2x + 12 = 90$$

$$2x = 78$$

$$x = 39$$

C A H

Angle E is 12° larger than angle D

Work out the length of DE.

$$DE = \frac{50}{\cos 39}$$

$$DE = 64.34$$

64.34

.....cm

(4)

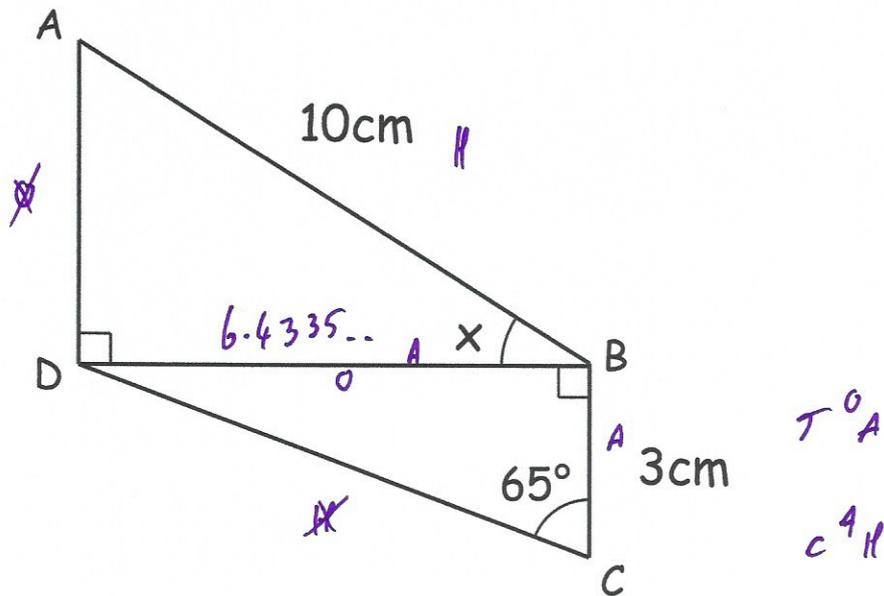
15. Two right-angled triangles are shown below.



AB is 10cm

BC is 3cm

Angle BCD is 65°



Calculate the size of angle ABD

$$\begin{aligned}BD &= \tan(65) \times 3 \\ &= 6.4335\dots\end{aligned}$$

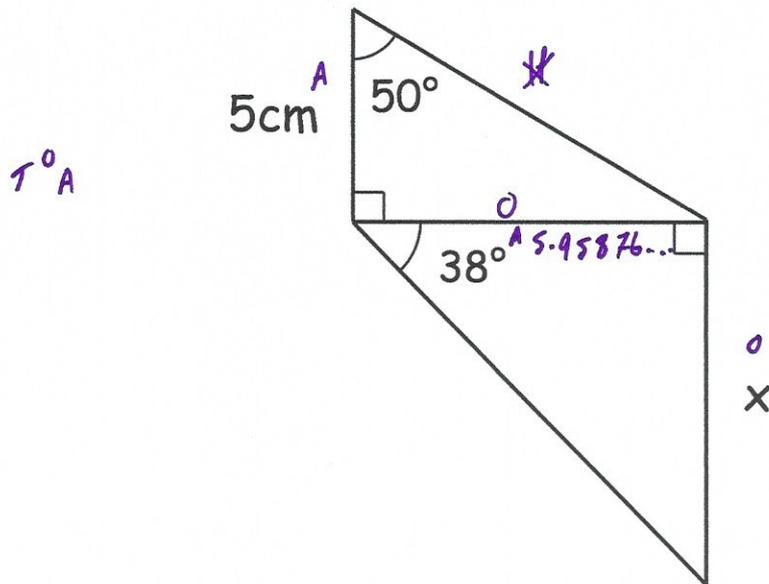
$$\cos x = \frac{6.4335\dots}{10}$$

$$\cos^{-1}\left(\frac{6.4335\dots}{10}\right) = 49.9577$$

$$\begin{array}{r}49.96 \\ \hline\end{array} \text{ }^\circ$$

(5)

14. The diagram shows two right-angled triangles.



Calculate the value of x .

$$\begin{aligned} \text{Opp} &= \tan(50) \times 5 \\ &= 5.958767\dots \end{aligned}$$

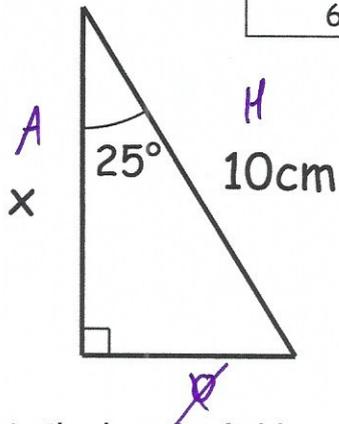
$$\begin{aligned} x &= \tan(38) \times 5.9587\dots \\ &= 4.655\dots \end{aligned}$$

$$\begin{aligned} &4.66 \text{ cm} \\ &\text{.....} \\ &(5) \end{aligned}$$

16. The diagram shows a right-angled triangle.



Angle	Sine	Cosine	Tangent
25°	0.423	0.906	0.466
65°	0.906	0.423	2.145



$C^A H$

$$x = \cos(25) \times 10$$

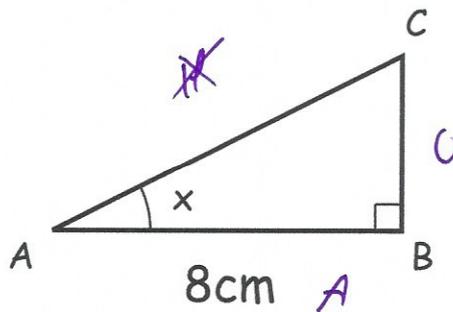
$$= 0.906 \times 10$$

$$= 9.06$$

Calculate the length of side x.

.....cm
(3)

17. ABC is a right-angled triangle.



$$\tan x = 0.6$$

Work out the length of BC

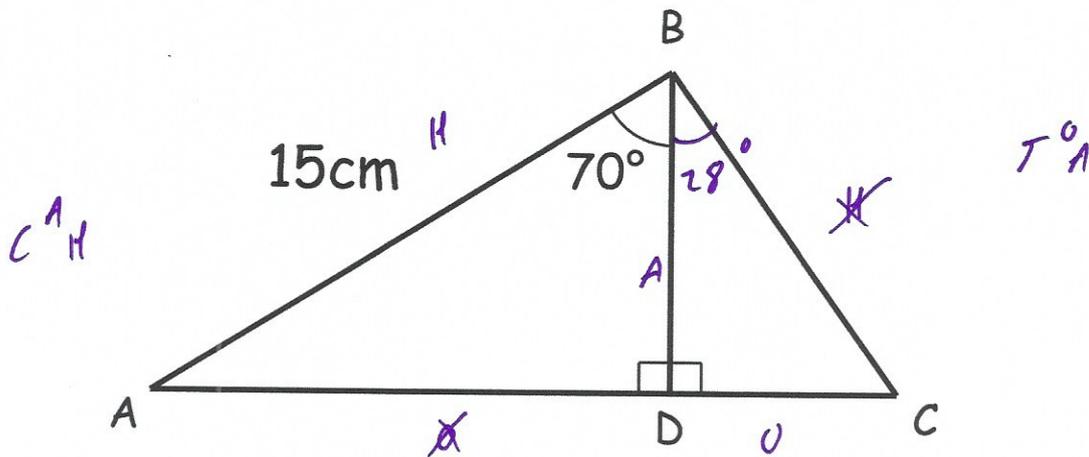
$$BC = \tan x \times 8$$

$$BC = 0.6 \times 8$$

$$= 4.8$$

.....cm
(3)

18. Shown below are right-angled triangles, ABD and BCD.



$AB = 15\text{cm}$

Angle $ABD = 70^\circ$

Angle $ABD : \text{Angle } DBC = 5 : 2$

$70 \div 5 = 14$

$14 \times 2 = 28$

Work out the length of CD

$$BD = \cos(70) \times 15$$

$$= 5.1303\dots$$

$$CD = \tan(28) \times 5.1303\dots$$

$$= 2.7278\dots$$

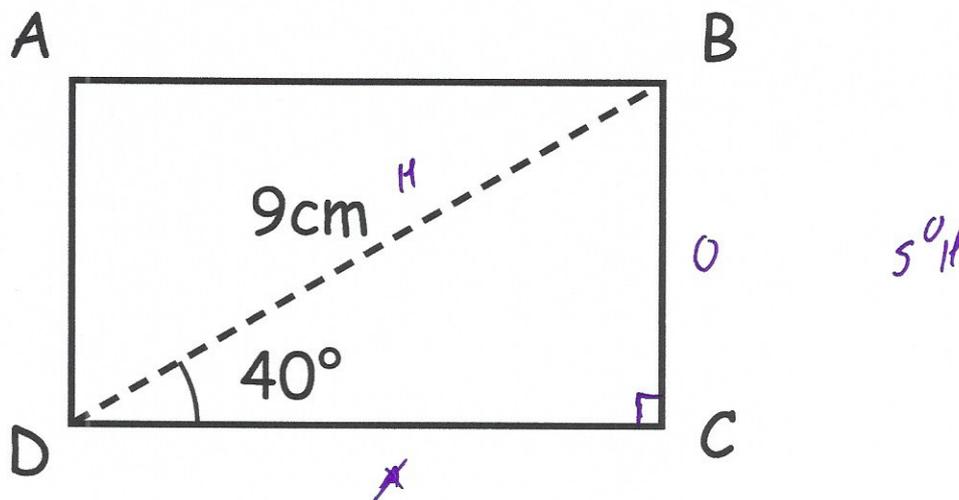
2.73
.....cm
(5)

19. ABCD is a rectangle.



BD = 9cm

Angle BDC = 40°



(a) Work out the length of BC

$$BC = \sin(40) \times 9$$

$$= 5.785048\dots$$

$$\dots\dots\dots 5.785 \text{ cm}$$

(2)

(b) Work out the perimeter of rectangle ABCD

$$BC^2 + CD^2 = BD^2$$

$$5.78508\dots^2 + CD^2 = 9^2$$

$$CD^2 = 47.5327512$$

$$CD = 6.89439\dots$$

$$\dots\dots\dots 25.36 \text{ to 2 dp.}$$

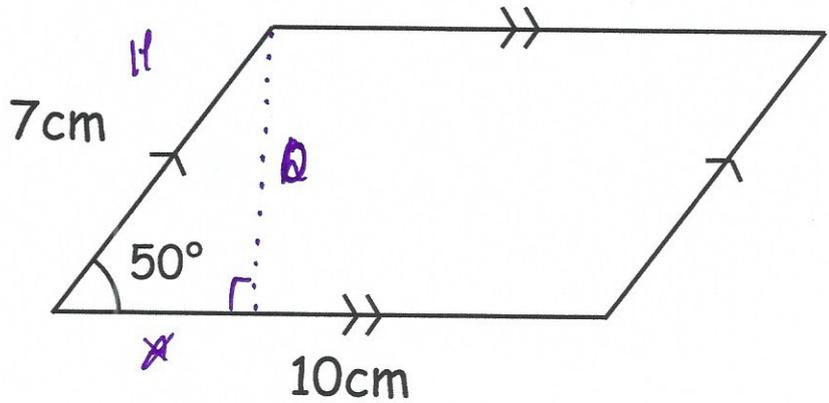
(3)

$$5.785 + 6.8944 + 5.785 + 6.8944 =$$

20. Shown below is a parallelogram.



5.011



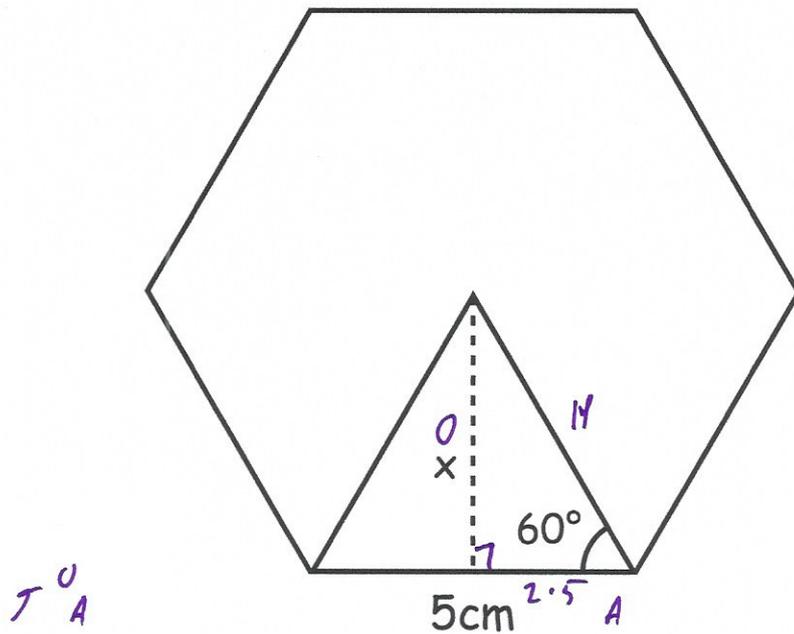
Calculate the area of the parallelogram.

$$h = \sin(50) \times 7$$
$$= 5.3623\dots$$

$$\text{Area} = b \times h$$
$$= 10 \times 5.3623\dots$$

53.62
.....cm²
(5)

21. A regular hexagon can be divided into 6 equilateral triangles.
The diagram below shows one of the equilateral triangles.



- (a) Use trigonometry to find the height, x , of the equilateral triangle.

$$x = \tan(60) \times 2.5$$

$$= 4.330127\dots$$

$$\dots\dots\dots 4.33 \text{ cm}$$

(3)

- (b) Calculate the area of the equilateral triangle.

$$\frac{1}{2} \times 5 \times 4.330\dots$$

$$\dots\dots\dots 10.8253 \text{ cm}^2$$

(1)

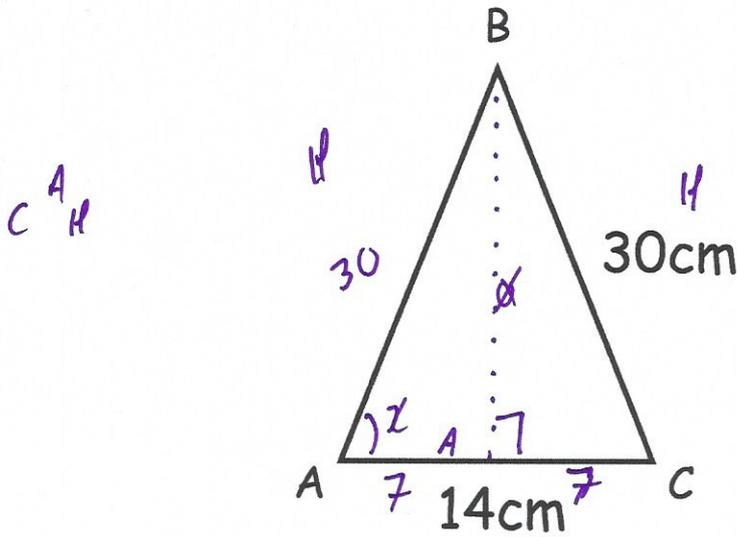
- (c) Calculate the area of the hexagon.

$$10.8253\dots \times 6$$

$$\dots\dots\dots 64.95 \text{ cm}^2$$

(1)

22. Shown below is isosceles triangle, ABC, where AB = BC



(a) Work out the size of angle BAC

$$\cos x = \frac{7}{30}$$

$$= 76.5066\dots$$

$$\underline{76.51}^\circ$$

to 2 dp. (3)

(b) Work out the size of angle ABC

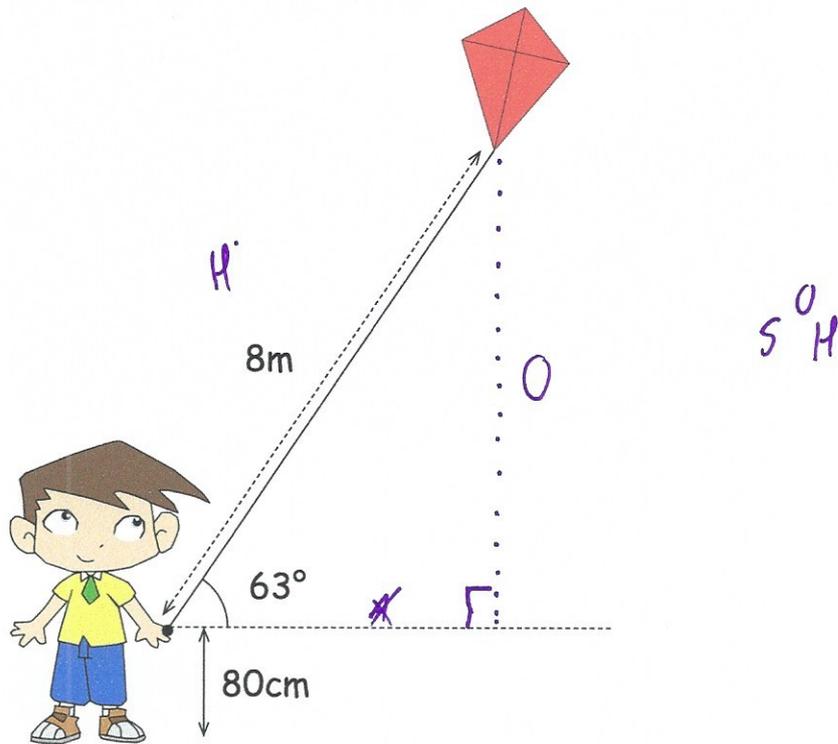
$$180 - 76.5066\dots - 76.5066\dots$$

$$= 26.9867\dots$$

$$\underline{26.99}^\circ$$

to 2 dp. (1)

23. Humphrey is flying a kite.



The handle is held 80cm above the ground.
The kite is on a string which is 8m long.
The string makes an angle of 63° with the horizontal.

Calculate the height of the bottom of the kite above the ground.

$$\begin{aligned} \text{Opp} &= \sin(63) \times 8 \\ &= 7.128 \text{ m} \end{aligned}$$

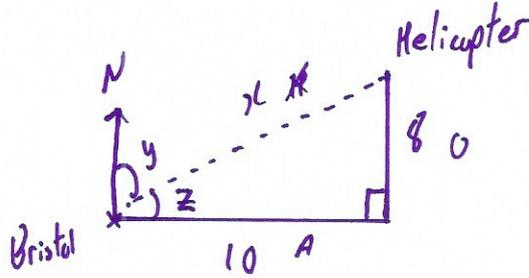
$$7.128 \text{ m} + 0.8 \text{ m}$$

$$\begin{aligned} &7.928 \\ &\text{.....m} \\ &\text{(4)} \end{aligned}$$

24. A helicopter leaves Bristol and flies due east for 10 miles. Then the helicopter flies 8 miles north before landing.



(a) Work out the direct distance of the helicopter from Bristol.



$$x^2 = 8^2 + 10^2$$

$$x^2 = 164$$

$$x = 12.806\dots$$

12.81 miles
(3)

(b) Calculate the bearing of the helicopter from Bristol.

$$\tan z = \frac{8}{10}$$

$$z = \tan^{-1}\left(\frac{8}{10}\right)$$

$$= 38.6598$$

$$y = 90 - 38.6598$$

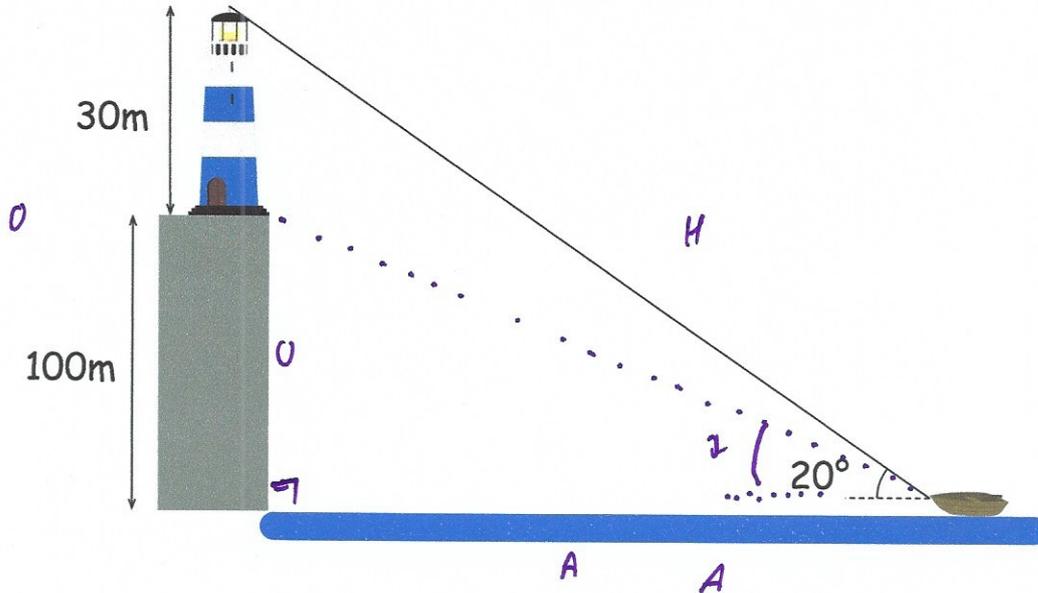
$$= 51.3402$$

051.34°
(3)

25. A boat is approaching a cliff with a lighthouse on top.



The cliff is 100m high and the lighthouse is 30m tall.



The angle of elevation from the boat to the top of the lighthouse is 20°

(a) Calculate the distance of the boat from the base of the cliff.

$T^0 A$

$$A = \frac{130}{\tan 20}$$

$$\underline{\underline{357.172}} \text{ m}$$

(3)

(b) Work out the angle of elevation from the boat to the top of the cliff.

$$\tan x = \frac{100}{357.172}$$

$$x = \tan^{-1} \left(\frac{100}{357.172} \right)$$

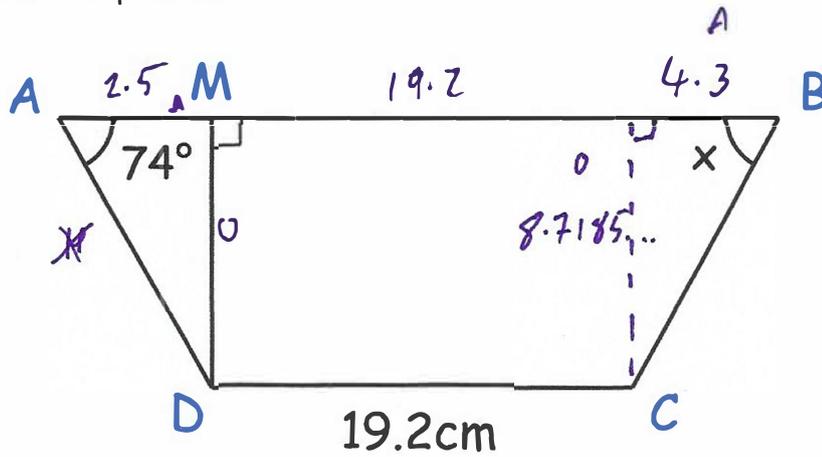
$$\underline{\underline{15.641}} \text{ }^\circ$$

(3)

26. ABCD is a trapezium



$T^0 A$



Angle BAD = 74°

CD = 19.2cm

AB = 26cm

AM = 2.5cm

Work out the size of angle ABC.

$$DM = \tan(74) \times 2.5$$

$$= 8.71853611\dots$$

$$\tan x = \frac{8.7185\dots}{4.3}$$

$$x = \tan^{-1}\left(\frac{8.7185\dots}{4.3}\right)$$

63.747°

.....
(5)