

Higher 2026 Paper 1

$$\begin{aligned} \textcircled{1} \quad 2x^2 + 20x + 3 &= p(x+q)^2 + r \\ &= p(x^2 + 2qx + q^2) + r \\ &= px^2 + 2pqx + pq^2 + r \end{aligned}$$

$$\begin{aligned} p &= 2 & 2pq &= 20 & pq^2 + r &= 3 \\ & & 4q &= 20 & 50 + r &= 3 \\ & & q &= 5 & r &= -47 \end{aligned}$$

$$\underline{\underline{2x^2 + 20x + 3 = 2(x+5)^2 - 47}}$$

$$\begin{aligned} 2x^2 + 20x + 3 &= 2[x^2 + 10x] + 3 \\ \text{or} \quad &= 2[(x+5)^2 - 25] + 3 \\ &= 2(x+5)^2 - 50 + 3 \\ &= \underline{\underline{2(x+5)^2 - 47}} \end{aligned}$$

3

$$\textcircled{2} \quad \int (15x^{2/3} + 7x^{-2}) dx$$

$$= \frac{15x^{5/3}}{5/3} + \frac{7x^{-1}}{-1} + C$$

$$= \underline{\underline{9\sqrt[3]{x^5}} - \frac{7}{x} + C}$$

4

$$\textcircled{3} \quad \text{centre } (-1, 2)$$

$$\begin{aligned} M_{\text{rad}} &= \frac{6-2}{2-(-1)} \\ &= \frac{4}{3} \end{aligned}$$

$$m_{\perp} = -\frac{3}{4}$$

$$6 = -\frac{3}{4}(2) + C$$

$$6 = -\frac{3}{2} + C$$

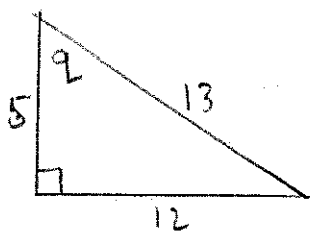
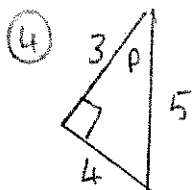
$$12 = -3 + 2C$$

$$C = \frac{15}{2}$$

$$y = -\frac{3}{4}x + \frac{15}{2}$$

$$\text{or } \underline{\underline{4y = -3x + 30}}$$

4



$$\textcircled{4} \quad (a) \quad \underline{\underline{\sin q = \frac{12}{13}}}$$

$$\sin p = \frac{4}{5}$$

$$\sin q = \frac{12}{13}$$

$$\cos p = \frac{3}{5}$$

$$\cos q = \frac{5}{13}$$

$$\begin{aligned} (b) \quad (i) \quad \sin(p+q) &= \sin p \cos q + \cos p \sin q \\ &= \frac{4}{5} \times \frac{5}{13} + \frac{3}{5} \times \frac{12}{13} \\ &= \frac{20}{65} + \frac{36}{65} \\ &= \underline{\underline{\frac{56}{65}}} \end{aligned}$$

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$$\begin{aligned} (c) \quad \tan(p+q) &= \frac{\sin(p+q)}{\cos(p+q)} \\ &= \frac{56}{65} \times -\frac{65}{33} \\ &= \underline{\underline{-\frac{56}{33}}} \end{aligned}$$

$$\begin{aligned} (ii) \quad \cos(p+q) &= \cos p \cos q - \sin p \sin q \\ &= \frac{3}{5} \times \frac{5}{13} - \frac{4}{5} \times \frac{12}{13} \\ &= \frac{15}{65} - \frac{48}{65} = \underline{\underline{-\frac{33}{65}}} \end{aligned}$$

$$\begin{aligned} \textcircled{5} \text{ (a) (i) } f(g(x)) &= f(x+3) \\ &= 2(x+3)^2 + 5 \\ &= 2(x^2 + 6x + 9) + 5 \\ &= 2x^2 + 12x + 18 + 5 \\ &= \underline{\underline{2x^2 + 12x + 23}} \end{aligned}$$

$$\begin{aligned} \text{(ii) } g(f(x)) &= g(2x^2 + 5) \\ &= 2x^2 + 5 + 3 \\ &= \underline{\underline{2x^2 + 8}} \end{aligned}$$

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$$\text{(b) } \underline{\underline{g(f(x)) \geq 8}}$$

$$\begin{aligned} \textcircled{6} \quad \vec{MN} &= \vec{MH} + \vec{HE} + \vec{EN} \\ &= -\frac{1}{2}\underline{\underline{u}} - \underline{\underline{v}} + \frac{1}{3}\underline{\underline{w}} \end{aligned}$$

2

$$\begin{aligned} \textcircled{7} \quad y &= 2x + 4x^{1/2} \quad \frac{dy}{dx} = 2 + 2x^{-1/2} \quad \text{when } x=9 \quad \frac{dy}{dx} = 2 + \frac{2}{\sqrt{9}} \\ &= 2 + \frac{2}{\sqrt{x}} \quad = 2 + \frac{2}{3} \\ &= \underline{\underline{\frac{8}{3}}} \end{aligned}$$

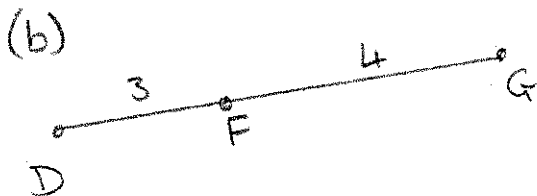
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$$\begin{aligned} \textcircled{8} \quad \log_2 x + \log_2 (x+2) &= 3 \\ \log_2 x(x+2) &= 3 \\ x^2 + 2x &= 2^3 \\ x^2 + 2x - 8 &= 0 \\ (x-2)(x+4) &= 0 \\ \downarrow \quad \quad \downarrow \\ \underline{\underline{x=2}} \quad \quad x=-4 \end{aligned}$$

4

$$\begin{aligned} \textcircled{9} \text{ (a) } \vec{DE} &= \underline{e} - \underline{d} = \begin{pmatrix} 1 \\ 2 \\ 7 \end{pmatrix} - \begin{pmatrix} -1 \\ 6 \\ 1 \end{pmatrix} = \begin{pmatrix} 2 \\ 0 \\ 10 \end{pmatrix} \\ \vec{EF} &= \underline{f} - \underline{e} = \begin{pmatrix} 2 \\ 0 \\ 10 \end{pmatrix} - \begin{pmatrix} 1 \\ 2 \\ 7 \end{pmatrix} = \begin{pmatrix} 1 \\ -2 \\ 3 \end{pmatrix} \\ &= \begin{pmatrix} 2 \\ -4 \\ 6 \end{pmatrix} = 2 \begin{pmatrix} 1 \\ -2 \\ 3 \end{pmatrix} = \begin{pmatrix} 1 \\ -2 \\ 3 \end{pmatrix} \end{aligned}$$

$2\vec{EF} = \vec{DE} \therefore EF \& DE$ are parallel.
Since there is a common point E,
D, E & F are collinear.



$$\begin{aligned} 4\vec{DF} &= 3\vec{FG} \\ 4(\underline{f} - \underline{d}) &= 3(\underline{g} - \underline{f}) \\ 4\underline{f} - 4\underline{d} &= 3\underline{g} - 3\underline{f} \end{aligned}$$

$$3\underline{g} = 7\underline{f} - 4\underline{d}$$

$$\underline{g} = \frac{1}{3}(7\underline{f} - 4\underline{d})$$

$$= \frac{1}{3} \left[7 \begin{pmatrix} 2 \\ 0 \\ 10 \end{pmatrix} - 4 \begin{pmatrix} -1 \\ 6 \\ 1 \end{pmatrix} \right]$$

$$= \frac{1}{3} \begin{pmatrix} 18 \\ -24 \\ 66 \end{pmatrix} = \begin{pmatrix} 6 \\ -8 \\ 22 \end{pmatrix}$$

$$\underline{\underline{G(6, -8, 22)}}$$

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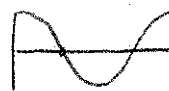
$$\textcircled{10} \int_{-\frac{\pi}{6}}^{\frac{\pi}{3}} 6 \sin\left(3x - \frac{\pi}{2}\right) dx$$

$$= \left[-\frac{6}{3} \cos\left(3x - \frac{\pi}{2}\right) \right]_{-\frac{\pi}{6}}^{\frac{\pi}{3}}$$

$$= \left(-2 \cos\left(\frac{3\pi}{3} - \frac{\pi}{2}\right) \right) - \left(-2 \cos\left(\frac{3\pi}{6} - \frac{\pi}{2}\right) \right)$$

$$= -2 \cos \frac{\pi}{2} + 2 \cos 0$$

$$= \underline{\underline{2}}$$



4

$$\textcircled{11} \text{(a) (i)} \quad \begin{array}{l|rrrr} x+2=0 & 1 & 7 & 18 & 16 \\ x=-2 & \downarrow & -2 & -10 & -16 \\ & 1 & 5 & 8 & 0 \end{array} \quad \text{Remainder} = 0 \therefore x+2 \text{ is a factor.}$$

$$\text{(ii)} \quad x^3 + 7x^2 + 18x + 16 = (x+2)(x^2 + 5x + 8)$$

linear factor

quadratic factor

$$\Delta = b^2 - 4ac$$

$$= 25 - 32$$

$$= -7$$

not a square number so does not factorise, so $(x+2)$ is the only linear factor.

$$\text{(b)} \quad 2x^3 + 20x^2 + 27x + 9 = 6x^2 - 9x - 23$$

$$2x^3 + 26x^2 + 36x + 32 = 0$$

$$(x+2)(x^2 + 5x + 8) = 0$$

$$\downarrow$$

$$x = -2$$

No real solutions

$$\text{When } x = -2, \quad y = 6(-2)^2 - 9(-2) - 23$$

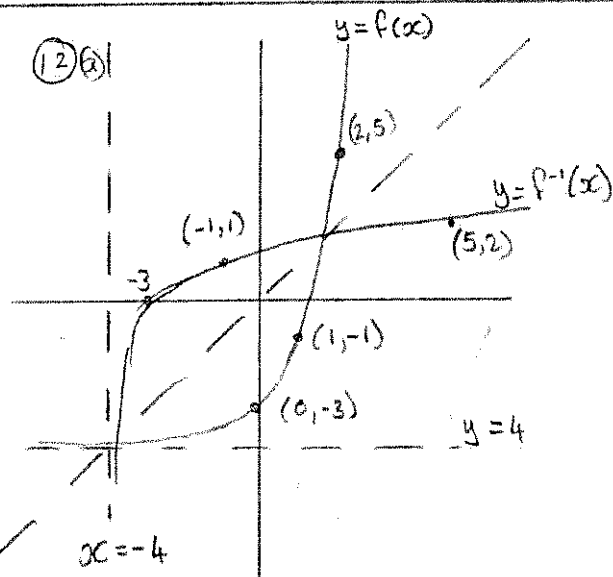
$$= 24 + 18 - 23$$

$$= 19$$

P.O.I. $(-2, 19)$

8

$\textcircled{12} \text{(a)}$



$$\text{(b) (i)} \quad y = \log_a(x+b)$$

$$\text{Sub } (-3, 0): \quad 0 = \log_a(-3+b)$$

$$1 = -3 + b$$

$$\underline{\underline{b = 4}}$$

$$\text{Sub } (5, 2): \quad 2 = \log_a(5+4)$$

$$2 = \log_a 9$$

$$a^2 = 9$$

$$\underline{\underline{a = 3}}$$

$$\text{(ii)} \quad \underline{\underline{x > -4}}$$

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