

## Functions 1

1.  $f(x) = 2x^2$  and  $g(x) = 5x - 4$ .

- (a) Find  $f(g(2))$ .
- (b) Find a formula for  $f(g(x))$ .

2.  $f(x) = \frac{2}{3x} - 1$  and  $g(x) = \frac{2}{3x + 3}$   $x \neq -1, 0$

- (a) Given  $h(x) = f(g(x))$ , find a formula for  $h(x)$ .
- (b) State the connection between  $f(x)$  and  $g(x)$ .

3.  $f(x) = 6x^2 - 4x$  and  $g(x) = \frac{1}{3x - 6}$ ,  $x \neq 2$

- (a) Show that  $g(f(x)) = \frac{1}{6(3x + 1)(x - 1)}$ .
- (b) State a suitable domain for  $g(f(x))$ .

4.  $f(x) = \frac{2}{1 - x}$  and  $g(x) = 1 - \frac{2}{x}$ ,  $x \neq 0, 1$

- (a) find  $f(g(x))$
- (b) State the connection between  $f$  and  $g$ .

5.  $f(x) = (x - 1)(x + 3)$  and  $g(x) = x^2 + 3$ .

Show that  $f(g(x)) - g(g(x)) = 2x^2$

6. The functions  $f$  and  $g$ , defined on suitable domains, are given by

$$f(x) = \frac{1}{x^2 - 4} \text{ and } g(x) = x + 1.$$

- (a) Find an expression for  $h(x)$ , where  $h(x) = f(g(x))$ .  
Give your answer as a single fraction.
- (b) State a suitable domain for  $h$ .

7. On a suitable set of real numbers, functions  $f$  and  $g$  are defined by

$$f(x) = \frac{1}{x+3} \text{ and } g(x) = \frac{1}{x} - 3$$

Find  $f(g(x))$  in its simplest form.

8. A function  $f$  is defined on the set of real numbers by  $f(x) = \frac{4-x}{x}$ ,  $x \neq 0$

Find in its simplest form an expression for  $f(f(x))$ .

9.  $f(x) = \frac{4}{x+2}$  and  $g(x) = \frac{2}{x} - 2$ ,  $x \neq -2, 0$

Find  $f(g(x))$  in its simplest form.

10.  $f(x) = \frac{x-5}{x}$  and  $g(x) = 3x - \frac{12}{x}$ ,  $x \neq 0$

(a) Show that  $f(g(x)) = \frac{(3x+4)(x-3)}{3(x-2)(x+2)}$

(b) State a suitable domain for  $f(g(x))$ .

11. Two functions are defined as  $f(x) = x^2 + 1$  and  $g(x) = 2 - x^2$ .

(a) Find an expression for  $f(f(x))$ .

(b) Find a similar expression for  $g(g(x))$  and hence show that  $f(f(x)) + g(g(x)) = 6x^2$ .

12.  $f(x) = 2x + 1$  and  $g(x) = x^2 + k$ , where  $k$  is a constant.

(a) Find an expression for (i)  $g(f(x))$  (ii)  $f(g(x))$ .

(b) Show that  $g(f(x)) - f(g(x)) = 0$  simplifies to  $2x^2 + 4x - k = 0$ .

(c) Find the value of  $k$  for which  $2x^2 + 4x - k = 0$  has equal roots.