

Sigma Notation General Practice

QUESTIONS

1. Evaluate

(a) $\sum_{r=1}^6 r$ (b) $\sum_{r=0}^3 r^3$ (c) $\sum_{k=1}^4 k^2$ (d) $\sum_{r=1}^7 r+6$ (e) $\sum_{t=0}^2 9-t^2$ (f) $\sum_{r=1}^9 2r+7$

2. Express each of these sums using sigma notation

(a) $1^2+2^2+3^2+4^2$ (b) $1^1+2^2+3^3+4^4+5^5$ (c) $1+x+x^2+x^3+x^4$
 (d) $1-x+x^2-x^3+x^4-x^5$ (e) $1-2+3-4+5-6$

ANSWERS

1. (a) 21 (b) 36 (c) 30 (d) 70 (e) 22 (f) 153

2. (a) $\sum_{k=1}^4 k^2$ (b) $\sum_{k=1}^5 k^k$ (c) $\sum_{k=0}^4 x^k$ (d) $\sum_{k=0}^5 (-x)^k$ (e) $\sum_{k=1}^6 (-1)^{k+1} k$

QUESTIONS

1. Write each of the following series in full

(a) $\sum_{k=1}^5 k^2$ (b) $\sum_{k=1}^9 (2k-1)$ (c) $\sum_{k=1}^{10} \frac{2520}{k}$

2. Express each of the following series in the form $\sum_{k=1}^n f(k)$

(a) $1+2+3+4+\dots+50$ (b) $5+10+15+\dots+30$
 (c) $3+5+7+9+11+13$

ANSWERS

1. (a) $1^2+2^2+3^2+4^2+5^2$ (b) $1+3+5+7+9+11+13+15+17$
 (c) $\frac{2520}{1} + \frac{2520}{2} + \frac{2520}{3} + \dots + \frac{2520}{10}$

2. (a) $\sum_1^{50} k$ (b) $\sum_1^6 5k$ (c) $\sum_1^6 2k+1$

