(a) Express $3 x^{2}+24 x+50$ in the form $a(x+b)^{2}+c$.
(b) Given that $f(x)=x^{3}+12 x^{2}+50 x-11$, find $f^{\prime}(x)$.
(c) Hence, or otherwise, explain why the curve with equation $y=f(x)$ is strictly increasing for all values of $x$.

Answers:
(a) $3(x+4)^{2}+2$
(b) $3 x^{2}+24 x+50$
(c) $\quad f^{\prime}(x)=3(x+4)^{2}+2$
$(x+4)^{2}>0$ for all values of $x$.
So $f^{\prime}(x)>0$ for all values of $x$.

