Higher Maths SQA 2023 Paper 1 Question 13



Functions f and g are defined by:

•
$$f(x) = 2\sin x$$
, where $0 < x < \frac{\pi}{2}$

•
$$g(x) = 2x$$
, where $0 < x < \frac{\pi}{4}$

(a) (i) Evaluate
$$f\left(g\left(\frac{\pi}{6}\right)\right)$$
.

(ii) Determine an expression for f(g(x)).

(b) (i) Given that
$$f(p) = \frac{1}{3}$$
, determine the exact value of $\sin p$.

(ii) Hence, determine the exact value of f(g(p)).

Answers:

(a) (i)
$$\sqrt{3}$$

(ii)
$$2 \sin 2x$$

(b) (i)
$$\frac{1}{6}$$

(ii)
$$\frac{\sqrt{35}}{9}$$