

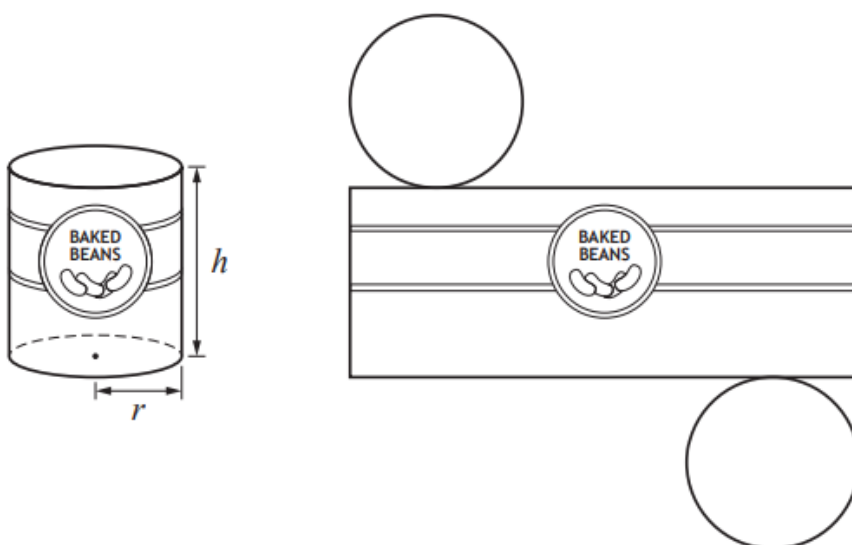
Higher Maths  
SQA 2021 Paper 2  
Question 9



A cylindrical tin of baked beans has a volume of  $450 \text{ cm}^3$ .

The radius of the tin is  $r \text{ cm}$  and its height is  $h \text{ cm}$ .

A net of the tin is shown in the diagram.



(a) Show that the surface area of the tin,  $A$  square centimetres, is given by

$$A(r) = 2\pi r^2 + \frac{900}{r}. \quad 3$$

(b) Determine the radius that will minimise the surface area. 6

Answers:

- (a) Obtain  $A(r, h) = 2\pi r^2 + 2\pi rh$   
Eliminate  $h$  using  $\pi r^2 h = 450$   
Obtain the required expression for  $A(r)$

- (b) minimum when  $r = \sqrt[3]{\frac{225}{\pi}}$