

Higher Maths
SQA 2019 Paper 2
Question 4



In a forest, the population of a species of mouse is falling by 2.7% each year.

To increase the population scientists plan to release 30 mice into the forest at the end of March each year.

- (a) u_n is the estimated population of mice at the start of April, n years after the population was first estimated.

It is known that u_n and u_{n+1} satisfy the recurrence relation $u_{n+1} = au_n + b$.

State the values of a and b .

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The scientists continue to release this species of mouse each year.

- (b) (i) Explain why the estimated population of mice will stabilise in the long term. 1
(ii) Calculate the long term population to the nearest hundred. 2

Answers:

(a) $a = 0.973, b = 30$

(b) (i) A limit exists as the recurrence relation is linear and $-1 < 0.973 < 1$.

(ii) 1100