Vectors $\mathbf{u}$ and $\mathbf{v}$ have components $\left(\begin{array}{c}p \\ -2 \\ 4\end{array}\right)$ and $\left(\begin{array}{c}2 p+16 \\ -3 \\ 6\end{array}\right), p \in \mathbb{R}$.
(a) (i) Find an expression for u.v.
(ii) Determine the values of $p$ for which $\mathbf{u}$ and $\mathbf{v}$ are perpendicular.
(b) Determine the value of $p$ for which $\mathbf{u}$ and $\mathbf{v}$ are parallel.

Answers:
(a) (i) $p(2 p+16)+30$ or equivalent
(ii) $\quad p=-5$ and $p=-3$
(b) $\quad p=-32$

