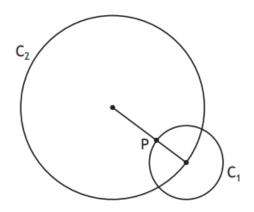
Higher Maths SQA 2018 Paper 2 Question 12



Circle C₁ has equation $(x-13)^2 + (y+4)^2 = 100$.

Circle C₂ has equation $x^2 + y^2 + 14x - 22y + c = 0$.



(a) (i) Write down the coordinates of the centre of C₁.

(ii) The centre of C_1 lies on the circumference of C_2 . Show that c=-455.

The line joining the centres of the circles intersects C_1 at P.

(b) (i) Determine the ratio in which P divides the line joining the centres of the circles.

(ii) Hence, or otherwise, determine the coordinates of P. 2

P is the centre of a third circle, C_3 .

C₂ touches C₃ internally.

(c) Determine the equation of C_3 .

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Answers:

(a) (i)
$$(13, -4)$$

(ii) Substitute coordinates and process for
$$c$$
.

(b) (i)
$$3:2 \text{ or } 2:3$$

(ii)
$$(5,2)$$

(c)
$$(x-5)^2 + (y-2)^2 = 1600$$
 or $x^2 + y^2 - 10x - 4y - 1571 = 0$