A quadratic function, $f$, is defined on $\mathbb{R}$, the set of real numbers.
Diagram 1 shows part of the graph with equation $y=f(x)$.
The turning point is $(2,3)$.
Diagram 2 shows part of the graph with equation $y=h(x)$.
The turning point is $(7,6)$.


Diagram 1


Diagram 2
(a) Given that $h(x)=f(x+a)+b$.

Write down the values of $a$ and $b$.
(b) It is known that $\int_{1}^{3} f(x) d x=4$.

Determine the value of $\int_{6}^{8} h(x) d x$.
(c) Given $f^{\prime}(1)=6$, state the value of $h^{\prime}(8)$.

Answers:
(a) $a=-5, b=3$
(b) 10
(c) -6

