Vectors $\mathbf{p}, \mathbf{q}$ and $\mathbf{r}$ are represented on the diagram as shown.

- $B C D E$ is a parallelogram
- $A B E$ is an equilateral triangle
- $|\mathbf{p}|=3$
- Angle $\mathrm{ABC}=90^{\circ}$

(a) Evaluate $\mathbf{p} \cdot(\mathbf{q}+\mathbf{r})$.
(b) Express $\overrightarrow{\mathrm{EC}}$ in terms of $\mathbf{p}, \mathbf{q}$ and $\mathbf{r}$.
(c) Given that $\overrightarrow{A E} \cdot \overrightarrow{E C}=9 \sqrt{3}-\frac{9}{2}$, find $|\mathbf{r}|$.

Answers:
(a) $4 \frac{1}{2}$
(b) $-\boldsymbol{q}+\boldsymbol{p}+\boldsymbol{r}$ or equivalent
(c) 6

