The function $f(x)=2^{x}+3$ is defined on $\mathbb{R}$, the set of real numbers.
The graph with equation $y=f(x)$ passes through the point $\mathrm{P}(1, b)$ and cuts the $y$-axis at Q as shown in the diagram.

(a) What is the value of $b$ ?
(b) (i) Copy the above diagram.

On the same diagram, sketch the graph with equation $y=f^{-1}(x)$.
(ii) Write down the coordinates of the images of $P$ and $Q$.
(c) $\mathrm{R}(3,11)$ also lies on the graph with equation $y=f(x)$.

Find the coordinates of the image of R on the graph with equation
$y=4-f(x+1)$.

Answers:
(a) $b=5$
(b) (i) Reflection in the line $y=x$.
(ii) $P(5,1) \quad Q(4,0)$
(c) $\mathrm{R}(2,-7)$

