## Essential Skills 5

The skills in this series of worksheets appear frequently.
These are the GIFTS you must take to succeed


## Stationary Points

Find the co-ordinates and determine the nature of the stationary points:

1. $y=x^{3}-3 x^{2}$
2. $f(x)=x^{3}-12 x$
3. $f(x)=x^{3}+9 x^{2}+24 x-18$
4. $y=2 x^{3}-7 x^{2}+4 x+4$
5. $y=2 x^{3}-3 x^{2}-36 x+17$
6. $\quad f(x)=x^{2}(2 x-3)$
7. $f(x)=x^{3}-2 x^{2}-4 x+1$
8. $y=(x-1)(x-2)^{2}$
9. $y=x\left(27-x^{2}\right)$
10. $f(x)=2 x^{2}\left(2-x^{2}\right)$

## APPLYING QUESTIONS



1. An open top box measures $x \mathrm{~cm}$ by $2 x \mathrm{~cm}$ and has a depth of $h \mathrm{~cm}$. The outer surface has an area of $216 \mathrm{~cm}^{2}$.
(a) Show that the volume of the cuboid is given by $V(x)=72 x-\frac{2}{3} x^{3}$
(b) Find the value of $x$ for which the volume is a maximum and calculate the volume.
2. A function $f$ is defined by $f(x)=x\left(x^{2}-3\right)$, where $0 \leq x \leq 3$.

Find the maximum and minimum values of $f$.

