

## Essential Skills 31

The skills in this series of worksheets appear frequently.

These are the GIFTS you must take to succeed



### Using the Natural Logarithm

Solve for  $x$ :

1.  $3^x = 18$
2.  $5^x = 90$
3.  $12^x = 3000$
4.  $4^{2x} = 35$
5.  $2^{3x-1} = 11$
6.  $0 \cdot 7^x = 0 \cdot 9$
7.  $7^{2-3x} = 5$
8.  $e^{0.6x} = 5 \cdot 2$
9.  $e^{-0.3x} = 0 \cdot 16$
10.  $50e^{-0.7x} = 45$



### APPLYING QUESTIONS

1. Evaluate  $\log_9 21$ , giving your answer to 2 decimal places.
2. A radioactive element decays according to the formula  $m_t = m_0 e^{-0.03t}$  where  $m_0$  is the initial mass and  $t$  is the time in years.
  - (a) What mass remains of the initial 200mg of the element after 40 years?
  - (b) What is the half-life of this element?
3. A colony of ants is estimated to be growing according to the formula  $P = 420e^{0.25t}$  where  $P$  is the population after  $t$  years.
  - (a) What was the initial population of ants?
  - (b) What is the population after 7 years?
  - (c) How long will it take the population to increase by a factor of 10?