## Essential Skills 30

The skills in this series of worksheets appear frequently. These are the GIFTS you must take to succeed

## Angle between Vectors

Calculate the angle between each pair of vectors:

- 1.  $\underline{u} = \underline{i} + 2\underline{j} + 3\underline{k}$  and  $\underline{v} = 4\underline{i} + \underline{j} + 5\underline{k}$
- 2.  $\underline{u} = 4\underline{i} + 2\underline{k}$  and  $\underline{v} = -2\underline{i} + 2j + 2\underline{k}$
- 3.  $\underline{u} = 3\underline{i} 2j + \underline{k}$  and  $\underline{v} = 5j \underline{k}$
- 4.  $\underline{u} = \underline{i} + \underline{j} + \underline{k}$  and  $\underline{v} = \underline{i} + 2\underline{j} 2\underline{k}$
- 5.  $\underline{u} = 2\underline{i} + 3\underline{j}$  and  $\underline{v} = -\underline{i} + 2\underline{j} + \underline{k}$
- 6.  $\underline{u} = 3\underline{i} + \underline{k}$  and  $\underline{v} = 2\underline{i} + 2j 7\underline{k}$
- 7.  $\underline{u} = 5\underline{i} + \underline{j} \underline{k}$  and  $\underline{v} = 2\underline{i} \underline{j} + 2\underline{k}$
- 8.  $\underline{u} = 2\underline{j} 6\underline{k}$  and  $\underline{v} = 3\underline{i} 2\underline{j} + 2\underline{k}$
- 9.  $\underline{u} = 7\underline{i} + \underline{j} \underline{k}$  and  $\underline{v} = 2\underline{i} \underline{j} + 3\underline{k}$
- 10.  $\underline{u} = \underline{i} 7\underline{j}$  and  $\underline{v} = \underline{i} + 4\underline{j} + \underline{k}$

## **APPLYING QUESTION**

- (a) C divides the line joining A (2, 1, -1) and B (8, 4, 8) in the ratio 2:1.Find the coordinates of C.
- (b) D has coordinates (9, -3, 11) and C divides  $\overrightarrow{DE}$  in the ratio 3:1 Find the coordinates of E.
- (c) Hence, calculate the size of angle BCE.



