## Essential Skills 30

The skills in this series of worksheets appear frequently.
These are the GIFTS you must take to succeed

## Angle between Vectors



Calculate the angle between each pair of vectors:

1. $\quad \underline{\boldsymbol{u}}=\underline{\boldsymbol{i}}+2 \underline{\boldsymbol{j}}+3 \underline{\boldsymbol{k}}$ and $\underline{\boldsymbol{v}}=4 \underline{\boldsymbol{i}}+\underline{\boldsymbol{j}}+5 \underline{\boldsymbol{k}}$
2. $\quad \underline{u}=4 \underline{i}+2 \underline{\boldsymbol{k}}$ and $\underline{v}=-2 \underline{i}+2 \underline{j}+2 \underline{\boldsymbol{k}}$
3. $\quad \underline{\boldsymbol{u}}=3 \underline{i}-2 \underline{j}+\underline{\boldsymbol{k}}$ and $\underline{v}=5 \underline{\boldsymbol{j}}-\underline{\boldsymbol{k}}$
4. $\quad \underline{\boldsymbol{u}}=\underline{i}+\underline{j}+\underline{\boldsymbol{k}}$ and $\underline{\boldsymbol{v}}=\underline{\boldsymbol{i}}+2 \underline{\boldsymbol{j}}-2 \underline{\boldsymbol{k}}$
5. $\quad \underline{\boldsymbol{u}}=2 \underline{i}+3 \underline{j}$ and $\underline{v}=-\underline{i}+2 \underline{j}+\underline{\boldsymbol{k}}$
6. $\underline{\boldsymbol{u}}=3 \underline{i}+\underline{\boldsymbol{k}}$ and $\underline{\boldsymbol{v}}=2 \underline{i}+2 \underline{\boldsymbol{j}}-7 \underline{\boldsymbol{k}}$
7. $\quad \underline{\boldsymbol{u}}=5 \underline{i}+\underline{\boldsymbol{j}}-\underline{\boldsymbol{k}}$ and $\underline{\boldsymbol{v}}=2 \underline{i}-\underline{\boldsymbol{j}}+2 \underline{\boldsymbol{k}}$
8. $\quad \underline{\boldsymbol{u}}=2 \underline{\boldsymbol{j}}-6 \underline{\boldsymbol{k}}$ and $\underline{\boldsymbol{v}}=3 \underline{\boldsymbol{i}}-2 \underline{\boldsymbol{j}}+2 \underline{\boldsymbol{k}}$
9. $\quad \underline{u}=7 \underline{i}+\underline{j}-\underline{k}$ and $\underline{v}=2 \underline{i}-\underline{j}+3 \underline{k}$
10. $\quad \underline{\boldsymbol{u}}=\underline{\boldsymbol{i}}-7 \underline{\boldsymbol{j}}$ and $\underline{\boldsymbol{v}}=\underline{\boldsymbol{i}}+4 \underline{\boldsymbol{j}}+\underline{\boldsymbol{k}}$

## APPLYING QUESTION

(a) $C$ divides the line joining $A(2,1,-1)$ and $B(8,4,8)$ in the ratio 2:1.

Find the coordinates of C .
(b) $\quad \mathrm{D}$ has coordinates $(9,-3,11)$ and C divides $\overrightarrow{D E}$ in the ratio 3:1 Find the coordinates of E .
(c) Hence, calculate the size of angle $B C E$.

