

Essential Skills 19

The skills in this series of worksheets appear frequently.

These are the GIFTS you must take to succeed

Proving Trigonometric Identities (Non Calculator)

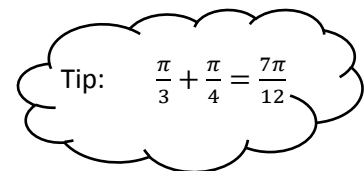


Prove that:

1. $\tan A - \tan B = \frac{\sin(A-B)}{\cos A \cos B}$
2. $(\sin A + \cos A)^2 = 1 + \sin 2A$
3. $\sin 3A = 3\sin A - 4\sin^3 A$
4. $\cos 3A = 4\cos^3 A - 3\cos A$
5. $(\cos A + \cos B)^2 + (\sin A - \sin B)^2 = 2(1 + \cos(A + B))$
6. $\sin^2 A = \frac{1}{2}(1 - \cos 2A)$
7. $\cos^2 A = \frac{1}{2}(1 + \cos 2A)$
8. $(\cos A + \sin A)(\cos A - \sin A) = \cos 2A$
9. $\frac{\sin(A-B)}{\cos A \cos B} = \tan A - \tan B$
10. $\cos(A - B) - \cos(A + B) = 2\sin A \sin B$

APPLYING QUESTIONS

1. (a) Prove that: $\frac{\cos(A+B)}{\cos A \cos B} = 1 - \tan A \tan B$
(b) Hence evaluate $\frac{\cos(\frac{7\pi}{12})}{\cos^{\frac{\pi}{3}} \cos^{\frac{\pi}{4}}}$



2. (a) Show that: $\cos(A + B) \cos(A - B) = \cos^2 B - \sin^2 A$
(b) Hence evaluate: $\cos\left(\frac{\pi}{6} + \frac{\pi}{4}\right) \cos\left(\frac{\pi}{6} - \frac{\pi}{4}\right)$